DiffCAD: Weakly-Supervised Probabilistic CAD Model Retrieval and Alignment from an RGB Image

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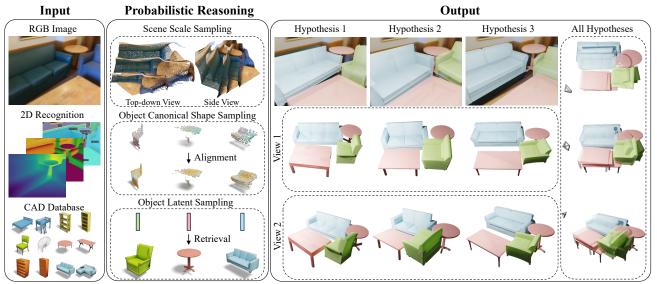


Figure 1. We introduce DiffCAD, a weakly-supervised approach for CAD model retrieval and alignment to a single RGB image. Unlike existing methods that require expensive CAD associations to real images for supervision, our approach is only trained on synthetic data, yet it can demonstrate superior performance on real-world datasets. We develop a probabilistic model to capture inherent depth/scale ambiguities in monocular 3D perception, leveraging diffusion to model 3D shape, pose, and scale for retrieval and alignment. DiffCAD predicts a plausible distribution of multiple candidate CAD retrieval and alignments for the objects in an RGB image.

Abstract

Perceiving 3D structures from RGB images based on CAD model primitives can enable an effective, efficient 3D object-based representation of scenes. However, current approaches rely on supervision from expensive annotations of CAD models associated with real images, and encounter challenges due to the inherent ambiguities in the task – both in depth-scale ambiguity in monocular perception, as well as inexact matches of CAD database models to real observations. We thus propose DiffCAD, the first weakly-supervised probabilistic approach to CAD retrieval and alignment from an RGB image. We formulate this as a conditional generative task, leveraging diffusion to learn implicit probabilistic models capturing the shape, pose, and scale of CAD objects in an image. This enables

multi-hypothesis generation of different plausible CAD reconstructions, requiring only a few hypotheses to characterize ambiguities in depth/scale and inexact shape matches. Our approach is trained only on synthetic data, leveraging monocular depth and mask estimates to enable robust zeroshot adaptation to various real target domains. Despite being trained solely on synthetic data, our multi-hypothesis approach can even surpass the supervised state-of-the-art on the Scan2CAD dataset by 5.9% with 8 hypotheses.

1. Introduction

Obtaining 3D perception from 2D input is a fundamental challenge in computer vision, with broad applications in robotics and human interaction with digital representations of the real world. While 2D semantic understanding from a single RGB image has achieved significant success in recent years [32, 40, 65, 68], 3D perception – required for enabling tasks such as navigation or interaction with objects – remains challenging, requiring not only object recognition but reconstruction of diverse, complex objects. In 3D perception, leveraging a CAD model basis for representing 3D objects in an image enables the use of a strong 3D prior on geometric structures as well as generates clean, compact mesh outputs directly compatible with modern rendering pipelines for downstream tasks.

While such CAD retrieval and alignment to generate an object-based 3D scene representation of real-world scene observation has shown strong promise [1, 31, 38, 42–44, 57], existing methods tend to rely on expensive CAD annotations to real images for supervision. Such annotations not only require trained annotators [1] but cannot produce exact ground truth matches in shape and pose, as synthetic CAD databases cannot tractably cover the distribution of general real objects, which introduces inherent ambiguities in the task. Moreover, this is further compounded by depth-scale ambiguity in monocular perception.

To address these challenges, we introduce DiffCAD, the first probabilistic approach for CAD retrieval and alignment to an RGB image that does not require any real-world supervision. To mitigate the multiple ambiguities inherent in monocular perception, we model the likely distributions of scene scale, object pose, and object shape as separate and disentangled conditional generative tasks. First, we employ a diffusion model to analyze potential scene scales based on an estimated monocular depth map. This enables considering multiple feasible solutions for object translation and scaling when subsequently solving for object poses. Given the estimated scales and depth map, we then model object pose through diffusion to predict an explicit canonical representation of objects, which we parameterize as normalized object coordinates (NOCs) [77]. The NOCs inform robust pose estimation and guide the diffusion of an object shape descriptor for CAD retrieval.

At inference time, we consider RGB images from real scenes. To help reduce the domain gap, we operate on machine-generated monocular depth and mask estimates from the RGB image (as photorealistic RGB generation from synthetic 3D data is challenging and expensive). We can then sample from our learned distributions for multiple plausible CAD reconstruction results. Our sampling scheme cascades from the scene-level diffusion, which offers potential scene scales. It then progresses to the explicit object representation diffusion, generating multiple NOCs that align with the scaled depth maps. Finally, it ends with the object latent diffusion, where the sampled latent vectors are used to query the CAD model database. This sampling scheme enables the generation of several CAD objects and

poses that capture shape and depth-scale ambiguity in representing the 3D scene depicted in an image.

Experiments on ScanNet [1, 17] images show that our learned probabilistic distributions well-capture likely CAD-based reconstructions, and with only 8 hypotheses, can even outperform fully-supervised state-of-the-art by 5.9%.

In summary, our contributions are:

- We propose the first probabilistic approach to CAD model retrieval and alignment from an RGB image, capturing inherent ambiguities due to depth-scale and lack of exact CAD matches in a database.
- We formulate our learned probabilistic model with diffusion processes that capture the distribution of scene scale, object pose, and object shape, with efficient sampling for multiple plausible hypotheses of CAD reconstructions.
- Our probabilistic approach leverages machineestimated depth and 2D masks, enabling robust generalization to real images while training only on synthetic data.

2. Related Work

2D Object Perception. With recent advancements in deep learning, significant progress has been achieved in various aspects of 2D object perception, including object detection [11, 24, 27, 32, 51], instance segmentation [28, 32, 40, 46, 49, 80], and reasoning about object and scene geometry, such as metric depth estimation [4, 8, 9, 30, 48, 63], and object normal map estimation [4, 21]. Our approach builds upon this progress in 2D recognition, leveraging segmentation and depth estimates to build a 3D understanding of the scene through probabilistic reasoning regarding scene scale, object pose, and shape.

Single-View Object Reconstruction. The task of inferring object shapes from images through reconstruction has gained significant attention in recent years. Researchers have explored a variety of explicit and implicit object representations, including voxel grids [16, 76], point clouds [23, 56, 82], polygonal meshes [29, 61, 78], and neural fields [18, 50, 58, 81]. Recent methods have also leveraged such single-view object reconstruction to construct scenes on an object basis [36, 53, 60, 84]. These approaches typically train on synthetic 3D shape data, producing flexible, underconstrained output representations, resulting in reconstructions that are typically over-tessellated (due to Marching Cubes) and often exhibit local noise (e.g., imperfect flat surfaces) or missing finer-grained structures, due to the high dimensionality of the output representation. In contrast, our approach leverages a stronger 3D prior by employing CAD model databases to directly model scene geometry, resulting in plausible object reconstructions up to

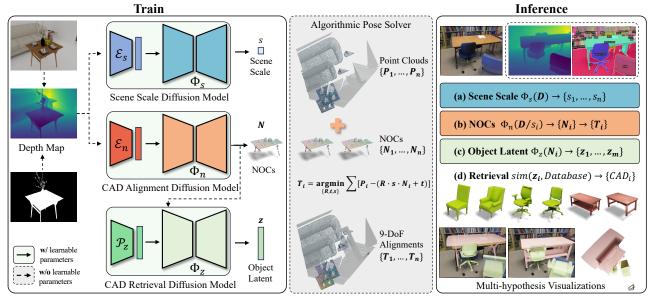


Figure 2. **Method Overview**. To facilitate multi-hypothesis reasoning for CAD model retrieval and alignment to a single image, we employ diffusion modeling over scene scale, object pose, and shape. From an input RGB image, we employ machine-generated estimates of depth and instance segmentation. From the estimated depth, we estimate scene scales with Φ_s . Φ_n uses the back-projected estimated depth of each detected object to output hypotheses for its Normalized Object Coordinates (NOCs). Φ_z then uses the estimated NOCs to predict the object shape as a latent vector that can be used for retrieval. Our probabilistic modeling also enables robust real-world CAD retrieval and alignment while training only on synthetic data.

the fidelity of the CAD database, and a compact representation directly suitable for downstream applications.

CAD Model Retrieval and Alignment. As CAD representations enable efficient, mesh-based representations of a scene, various methods have explored CAD retrieval and alignment to real-world RGB images [31, 38, 42-44] as well as RGB video [57] and RGB-D scans [1–3, 7, 20]. For the challenging task of single-view RGB input, early methods have relied on the availability of ground truth scale information [42, 43] for full 9-DoF 3D reconstruction. Recent works have also proposed to directly learn metric depth estimation within the target domain [31, 44, 45]. These methods all not only rely on ground truth supervision in the target domain, which is expensive and inexact to acquire, but produce deterministic outputs, whereas the task setting is inherently ambiguous due to depth-scale ambiguity and inexact CAD matches. In contrast, we propose a probabilistic approach to effectively model multiple plausible hypotheses, and maintain general applicability to real images while trained only on synthetic data.

Diffusion Models. Recently, diffusion models [34, 39, 67, 71, 73] have shown remarkable success in modeling image generation while employing an implicit probabilistic model. Due to their success in generative modeling of RGB images, recent works have shown more general applicabil-

ity to various tasks, including segmentation [5, 80], keypoint matching [33, 55, 75], retrieval-based image generation [10, 13, 69], and 3D shape generation [14, 22, 41, 47, 59, 70, 82, 83, 86]. We propose to employ diffusion modeling to characterize probabilistic models of scenes, along with CAD shape and pose for CAD model reconstruction of a single-view image.

3. Method

3.1. Overview

Given an RGB image I and a database of n CAD models $\{O_i\}_{i\in[1,n]}$, our goal is to represent objects in the scene by combining CAD models from the database with a set of 9-DoF transformations $\{\mathbf{T}_i\}_{i\in[1,n]}$ that align these models to the metric camera space, forming a compact, object-based 3D scene representation.

Figure 2 shows an overview of our method. We propose a combination of disentangled diffusion models to probabilistically model ambiguities in monocular perception and shape matching. Specifically, we model scene scale Φ_s , pose prediction Φ_n , and CAD model retrieval Φ_z as diffusion processes to effectively capture likely CAD model reconstructions of an image.

To reason robustly across various domains, we operate on machine-generated depth \mathbf{D} and semantic instance masks estimated from \mathbf{I} , denoted as \mathbf{D}_p indicating the masked depth estimate of each object (object index left out

for simplicity of notation).

We start by addressing the scene-level depth-scale ambiguity. We learn the distribution of potential scales within the scene with a diffusion model Φ_s , conditioned on \mathbf{D} . We can then sample scales $\{s_i\}_{i\in[1,n]}$ from Φ_s , to produce the most likely metric scenes $\{\mathbf{D}_i=\frac{1}{s_i}\mathbf{D}\}_{i\in[1,n]}$. This enables us to facilitate multiple reasonable transformations of objects.

We then model the object pose with diffusion model Φ_n , which estimates the normalized object coordinates (NOCs) [77] conditioned on the back-projected point clouds \mathbf{P} of \mathbf{D}_p . The 9-DoF pose is recovered through RANSAC [25].

Given the estimated object pose characterized through NOCs, we also predict the object shape represented as a latent shape code through diffusion model Φ_z . This probabilistic model enables capturing a distribution of possible matches, which enables more robust shape retrieval in real scenarios where no exact match from the database exists.

3.2. Diffusion Models

This work follows the denoising diffusion probabilistic models (DDPMs) formulation [35] to model CAD model retrieval and alignment from a single image, including the scene scale s, NOCs N, and the latent object shape z.

Given a data distribution q(x), we denote a sampled data point as x_0 . The *forward process* iteratively injects Gaussian noise to transform x_0 to x_T , which fits an isotropic Gaussian in T timesteps, by a Markovian process [35, 72]:

$$q(x_t|x_{t-1}) = \mathcal{N}(x_t; \sqrt{1 - \beta_t} x_{t-1}, \beta_t \mathbf{I}), \qquad (1)$$

$$q(x_{1:T}|x_0) = \prod_{t=1}^{T} q(x_t|x_{t-1}), \tag{2}$$

where $t \in [1, T]$ and β_t is a pre-defined variance schedule.

The denoising neural network Φ learns to fit $p_{\Phi}(x_{t-1}|x_t)$ that can approximate $q(x_t|x_{t-1},x_0)$ to and thus recover the x_0 by the *reverse process*:

$$p_{\Phi}(x_{t-1}|x_t) = \mathcal{N}(x_{t-1}; \mu_{\Phi}(x_t, t), \Sigma_{\Phi}(x_t, t)),$$
 (3)

$$p_{\Phi}(x_{0:T}) = p(x_T) \prod_{t=1}^{T} p_{\Phi}(x_{t-1}|x_t).$$
 (4)

We can thus train our diffusion models Φ_s , Φ_n , and Φ_z following ϵ -formulation [35, 67] or directly optimize for x_0 following [15, 64] to recover individual data distributions.

3.3. Φ_s : Scene Scale Diffusion

As monocular perception inherently contains depth-scale ambiguity, we use Φ_s to model likely scene scales. Since we condition on a machine-generated depth \mathbf{D} , we model this as the scale difference from the predicted depth. We define the target scale difference between the predicted depth

map \mathbf{D} and the reference depth map \mathbf{D}_{gt} as follows:

$$s_{gt} = \operatorname{avg}\left(\frac{\mathbf{D} \odot \mathbf{M}}{\mathbf{D}_{gt} \odot \mathbf{M}}\right). \tag{5}$$

Here, M represents the mask of the target object, and \odot denotes the Hadamard product.

 Φ_s is conditioned on features extracted from estimated depth map **D** from a pre-trained ResNet-50-FCN backbone [54]. Since the defined scene scale target is an isotropic scalar that zooms the initial estimates uniformly in each direction, we construct the scale diffusion target vector **S** with each element equals to $s_{\rm gt}$ and has the same size as the depth feature map, and concatenate them as input to the model. We adopt the objective function proposed in [35] for training the diffusion U-Net Φ_s :

$$\mathcal{L}_s = \mathbb{E}_{\epsilon \sim \mathcal{N}(0,I),t} \Big[||\epsilon - \epsilon_{\Phi_s}(t)||_1 \Big]. \tag{6}$$

At inference time, we sample S by denoising a noise sample from the standard normal distribution, conditioned on D, and take s = avg(S) as the isotropic scale factor. The re-scaled depths offer multiple hypotheses for plausible object translation and scale to bring the object from its canonical space to metric camera space.

3.4. Φ_n : CAD Alignment Diffusion

 Φ_n models a distribution over likely object poses. We define the 9-DoF transformation as $\mathbf{T} = [\mathbf{R}|\mathbf{t}|\mathbf{s}]$, where $\mathbf{R} \in \mathbf{SO}(3)$ represents rotation, $\mathbf{t} \in \mathbb{R}^3$ translation, and $\mathbf{s} = (s_x, s_y, s_t)^T$ anisotropic scale. Instead of modeling this explicit pose representation, which must consider the different spaces for rotation, translation, and scale, we predict the normalized object coordinates (NOCs) [77] \mathbf{N} of the object. The NOC representation provides geometric correspondences between the observed object and its canonical coordinate system, enabling solving for \mathbf{T} as well as more generalized learning across different object shapes. As NOCs \mathbf{N} are structured geometrically similarly to the back-projected points \mathbf{P} of \mathbf{D}_p , we condition their prediction on \mathbf{P} .

Features \mathbf{P}_f are extracted from condition \mathbf{P} using the 3DGC backbone [52]. Φ_n then operates on a concatenation of the target NOCs with their corresponding per-point features from \mathbf{P}_f . The objective is to minimize the difference between predicted and ground truth noise, formulated as:

$$\mathcal{L}_n = \mathbb{E}_{\epsilon \sim \mathcal{N}(0,I),t} \Big[||\epsilon - \epsilon_{\Phi_n}(t)||_1 \Big]. \tag{7}$$

During inference, NOC candidates are sampled from Gaussian noise, conditioned on P_f . We can then solve for the 9-DoF object transformation T from the NOC estimates using a pose solver following a similar approach as presented in CaTGrasp [79], which is computed via

RANSAC [25] to find the transformation from the predicted NOCs and the observed point cloud **P**.

3.5. Φ_z : CAD Retrieval Diffusion

Given our estimated NOCs capturing the visible geometry of the object mapped to its canonical space, we use this information to estimate the 3D shape for retrieval from a CAD database. As explicit 3D shape representations (e.g., voxels, points) are quite high-dimensional, we employ a latent space representation of objects, with latent codes $\mathbf{z} \in \mathbb{R}^d$.

To compress the shape into latent space, we opt for an architecture similar to ConvONet [62], denoted as Φ_o . We modify the encoder to produce a global feature vector representing each object, with a dimension of \mathbb{R}^d . We pre-train Φ_o to encode the CAD models with reconstruction loss following [62]. The samples in the latent space in which the Φ_z learns to sample from are extracted from the encoding of the CAD database using Φ_o .

To encode the information captured by the NOC estimate N, we learn a positional feature embedding that maps point locations of N from \mathbb{R}^3 to \mathbb{R}^C together with a single-layer MLP that serves as the context of the condition for Φ_z . Φ_z then learns to denoise the object latent vector at each timestep. We fellow recent works [15, 64] and directly optimize for the original denoised latent vector \mathbf{z}_0 :

$$\mathcal{L}_z = ||\Phi_n(\mathbf{z}_t) - \mathbf{z}_0||_1. \tag{8}$$

During inference, we sample the object latent vector \mathbf{z} and query the CAD database to retrieve the nearest neighbor based on cosine similarity.

3.6. Synthetic Dataset Augmentation

We train our approach on a synthetic 3D scene dataset 3D-FRONT [26] to capture various scene scales, object arrangements, and shapes. However, this process can be prone to overfitting because the original 3D-FRONT scene configuration only contains 1,334 unique objects (for our target classes). To better capture a wider distribution of possible objects and arrangements, we further inject information from other existing large synthetic object databases, such as ShapeNet [12]. We consider the shape database of objects from 3D-FUTURE and those of ShapeNet, yielding 18,229 objects. We then augment the synthetic 3D scenes by replacing existing furniture with unused CAD models randomly retrieved from the same category in the database. This enables learning from more diverse object shapes and arrangements.

Our augmented synthetic dataset comprises \approx 300k images spanning 6 target categories.

3.7. Multi-Hypothesis Sampling from an Image

Since 3D CAD retrieval and alignment from a single view brings inherent ambiguities in terms of depth-scale, object shape, and pose, our approach addresses the ambiguities by a hierarchical multi-candidate sampling scheme. Our inference process begins by employing off-the-shelf 2D recognition backbones [9, 21, 80] to derive depth, mask, and normal estimates from the input image I. Subsequently, we sample in a cascaded fashion from our trained diffusion models, progressing from scene-level reasoning to sampling explicit object representations and ending with the prediction of implicit object representations.

Initially, we sample a set of n potential scales, denoted as $\{s_i\}_{i\in[1,n]}$, from Φ_s based on the predicted depth map \mathbf{D} from \mathbf{I} . NOC candidates are then sampled at each scene scale, $\{\mathbf{N}_i\}_{i\in[1,n]}$, given each scaled depth map, from Φ_n . The corresponding 9-DoF transformations $\{\mathbf{T}_i\}_{i\in[1,n]}$ are computed using a RANSAC-based solver [25]. The possible latent candidates for objects, \mathbf{z}_i , are sampled conditionally on \mathbf{N}_i from the Φ_z . We sample m object candidates given each \mathbf{N}_i and conduct a nearest neighbor search in the CAD model database to retrieve CAD models based on the cosine similarity between latent vectors.

The hierarchical sampling approach generates $\{n \times m\}$ samples corresponding to various scene scales. For each scene scale s_i , a simple hypothesis ranking scheme selects the best candidate by rendering the normals of those CAD models using the solved poses \mathbf{T}_i and computing the similarity between the rendered normal and the machine-estimated normal from RGB input using LPIPS [85]. The selection criterion is based on the model with the lowest LPIPS error, resulting in n sets of CAD models that align with the probabilistically permuted scenes.

Implementation Details. For Φ_s , we use a learning rate of $5e^{-5}$ and batch size 64, on a single RTX a6000 GPU for 2 days. For Φ_n , we condition on subsampled point clouds with 1024 points, using learning rate $5e^{-5}$ on a single RTX a6000 GPU with a batch size of 96, spanning 3 days per category. Φ_o is trained on a single a100 GPU with a batch size of 128 for 3 days, with a learning rate $1e^{-4}$. We then train Φ_z on an RTX a6000 GPU with batch size 128 and learning rate $1e^{-4}$, for 3 days per category.

4. Experiments

We demonstrate the effectiveness of our weakly-supervised approach on real-world ScanNet [17] and ARKit [6] data. As Scan2CAD [2] provides ShapeNet [12] annotations to ScanNet scenes, we evaluate CAD alignment accuracy and retrieval on the ScanNet25k image data, which contains 5k validation images. In the absence of CAD annotations for ARKit, we present a qualitative-only evaluation on ARKit.

4.1. Evaluation Metrics

Alignment Accuracy. We introduce a new alignment evaluation protocol for single-view CAD alignment and re-

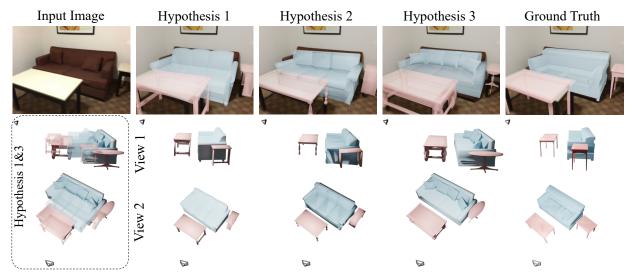


Figure 3. **Qualitative Results on ScanNet [1, 17].** Our probabilistic approach shows multi-feasible sets of object shape and pose pairs given the ambiguities in monocular perception. Left-bottom: The two hypotheses corresponding to the smallest and largest scene scale reconstructions follow possible depth-scale ambiguity from the camera view.



Figure 4. **Qualitative Comparison on ScanNet [1, 17].** Our weakly-supervised probabilistic approach produces more representative retrieval and alignment, even under strong occlusions (bottom), compared with in-domain supervised methods [31, 44].

trieval. We observe that previous methods [31, 44, 57] adopted a similar evaluation protocol to Scan2CAD [2], which operates on reconstructed scenes, and thus aggregate predictions over multiple frames per scene. Instead, we aim to evaluate the performance given only a single RGB image. We thus compute alignment accuracy following the same thresholds as in prior work [1, 31, 44, 57], but only considering a single RGB frame as input: an alignment is

correct if the predicted object class is correct, translation error < 20cm, rotation error $< 20^{\circ}$, and scale ratio < 20%.

As multiple hypotheses should reflect a distribution from which the ground truth is likely to appear, we evaluate multiple hypotheses from each method by evaluating how close the ground truth lies to any hypothesis, that is, the hypothesis with the minimum error as follows:

$$e = \arccos\left(\frac{\operatorname{tr}\left(\hat{\mathbf{R}}\mathbf{R}_{gt}^{T}\right) - 1}{2}\right) + ||\hat{\mathbf{t}} - \mathbf{t}_{gt}||_{2} + ||\frac{\hat{s}}{s_{gt}} - 1||_{1},$$
(9)

where $(\hat{\cdot})$ denotes predictions.

Retrieval Similarity. To evaluate the shape retrieval, we establish the retrieval similarity as the L1 Chamfer Distance between point clouds sampled from the retrieved mesh and the corresponding ground truth. We set the candidate CAD models for retrieval as the 1943 models that appear in the Scan2CAD [1] training set. A total of 10k points are sampled on the meshes for evaluation. To evaluate our method probabilistically, we report the candidate with the minimum L1 Chamfer Distance according to the ground truth.

4.2. Comparison to State of the Art

Tab. 1 compares our weakly-supervised method with state-of-the-art single-frame-based methods ROCA [31] and SPARC [44], both of which require full supervision, on ScanNet [1, 17]. As the single image setting can contain depth-scale ambiguities, we evaluate multiple hypotheses for methods that allow so. ROCA is fully deterministic, and so only provides one hypothesis. While SPARC was not developed for multi-hypothesis reasoning, multiple samples can be drawn from different initialization angles (always in-

Method	in-domain supervision	#hypotheses	bed	bkshlf	cabinet	chair	sofa	table	avg↑
ROCA [31]	1	-	11.2	11.3	12.6	35.8	8.7	9.3	14.8
SPARC [44]	✓	1	26.1	21.7	27.8	47.4	25.9	19.7	28.1
SPARC [44]	✓	8	26.7	24.6	28.8	48.9	28.9	24.1	30.3
SPARC [44]	✓	12	28.6	25.6	29.8	49.3	31.2	25.0	31.6
SPARC [44]	✓	16	29.2	<u>26.1</u>	30.5	49.6	31.9	26.4	32.3
SPARC [44]	✓	20	29.8	27.1	30.8	49.8	32.7	<u>26.8</u>	32.8
Ours	Х	1	13.0	4.4	9.6	22.4	13.3	4.9	11.3
Ours	X	8	28.6	16.7	32.8	55.0	41.1	18.6	32.1
Ours	Х	12	30.4	20.2	35.1	58.5	41.1	21.6	34.5
Ours	X	16	<u>31.1</u>	21.7	<u>39.4</u>	<u>61.3</u>	<u>44.9</u>	24.8	<u>37.2</u>
Ours	Х	20	32.9	24.1	42.1	62.5	47.5	27.1	39.4

Table 1. **Alignment Accuracy on ScanNet [1, 17]** in comparison to state-of-the-art approaches, which require in-domain ground truth supervision. While SPARC [44] has not been developed for probabilistic reasoning, multiple hypotheses can be generated by sampling different initialization angles (always including those obtained with the officially released initialization angle). Evaluation under the same #hypotheses are colored in 8, 12, 16, and 20 hypotheses. Our probabilistic approach can outperform fully-supervised methods, while reflecting a more likely distribution of poses.

cluding the authors' proposed initialization angle).

DiffCAD learns a much more representative distribution, surpassing fully-supervised state of the art with only 8 hypotheses, reflecting the quality of our learned distribution. Performance increases with more hypotheses, with a marginal saturation of around 20 hypotheses. In contrast, the performance of SPARC only increases very marginally with increasing sampled hypotheses.

Tab. 2 evaluates CAD retrieval similarity compared to the state-of-the-art. Since SPARC uses the same deterministic retrieval as ROCA, multiple hypotheses are not available for either method. With our probabilistic modeling, DiffCAD performs on par with state-of-the-art with one hypothesis and significantly improves with more hypotheses, better reflecting likely shape reconstructions, even with only weak supervision available.

In Fig. 4, we show a qualitative comparison of CAD retrieval and alignment on ScanNet images. DiffCAD achieves more accurate object retrieval and alignments across a diverse set of image views and object types, due to our effective probabilistic modeling, compared with in-

domain supervised methods.

Evaluation on ARKit Our approach can be applied to various real-world images, as shown in Fig. 5 for ARKit [6] data, despite training only on synthetic data.

4.3. Ablations

How effective are our learned distributions compared to non-parametric sampling? We consider our learned probabilistic distributions in comparison with alternative non-parametric sampling schemes. We study this for Φ_s , as we can employ a straightforward sampling baseline: we estimate the mean μ' and variance σ'^2 of scale offsets between predicted and ground truth train depth maps, and instead draw samples from $\mathcal{N}(\mu', \sigma')$ (denoted as 'Smart Random Sampling (SRS)' in Fig. 6). Fig. 6 illustrates that our scene scale diffusion model Φ_s significantly outperforms SRS with much higher sampling efficiency.

Predicting NOCs in comparison with explicit transformation estimation of T. Tab. 3 shows that our NOC-based proxy for alignment estimation enables much more robust

Method	in-domain supervision	#hypotheses	bed	bkshlf	cabinet	chair	sofa	table	avg↓
ROCA [31]	✓	-	0.087	0.089	0.130	0.100	0.099	0.132	0.106
SPARC [44]	✓	-	0.087	0.089	0.130	0.100	0.099	0.132	0.106
Ours	Х	1	0.117	0.108	0.115	0.115	0.093	0.145	0.116
Ours	×	8	0.075	0.064	0.079	0.075	0.066	0.089	0.075
Ours	X	12	0.065	0.060	0.074	0.069	0.062	0.083	0.069
Ours	X	16	0.061	0.057	0.071	0.066	0.060	0.077	0.065
Ours	X	20	0.058	0.055	0.069	0.064	0.058	0.072	0.063

Table 2. **Retrieval Similarity on ScanNet** [1, 17] compared to in-domain supervised state-of-the-arts methods. Note that SPARC [44] uses the same retrieval provided by ROCA [31]. Evaluation under the same #hypotheses are colored in 8, 12, 16, and 20 hypotheses. Our approach matches the performance of state of the art with 1 hypothesis, and reflects a likely distribution, retrieving more accurate objects with only a few hypotheses.

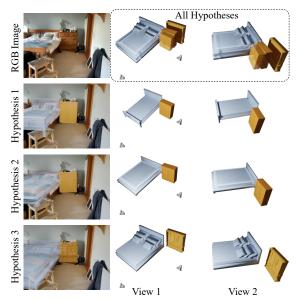


Figure 5. **Qualitative Results on ARKit [6].** Our method can be applied with multi-hypothesis reasoning to various real-world indoor datasets.

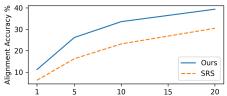


Figure 6. Scale Sampling Ablation. Our learned probabilistic model for Φ_s shows much higher sampling efficiency than non-parametric sampling.

alignment than the direct prediction of the 9-DoF values of $\bf T$. The NOC proxy estimation enables more robust estimation through its dense correspondences, which also helps mitigate the potential domain gap between synthetic training data and real-world test scenarios. We consider two alternatives to explicit $\bf T$ prediction: ' Φ_n + P' predicts 9-DoF values of $\bf T$ along with NOCs, and ' Φ_n + S' predicts only object scale along with NOCs. We evaluate both for the explicit pose prediction as well as for the pose solved by the NOCs via the solver, and select the one with lower error according to Eq. 9. Our approach to leveraging NOCs and an algorithmic pose solver achieves significantly better cross-domain alignment accuracy.

What is the effect of using the canonical object representation for retrieval? We consider performing CAD retrieval in the camera space of the image and the canonical space of the CAD database in Tab. 4. We consider a baseline alternative, ' Φ_z +PC', which operates on features from the back-projected point cloud in camera space as the retrieval condition. Learning the shape feature embeddings in

Method	#hypotheses	Alignment Accuracy↑
$\Phi_n + P$	8	16.3
$\Phi_n + S$	8	19.9
Φ_n w/o Aug	8	25.8
Ours	8	32.1

Table 3. Pose estimation ablation. With synthetic data replacement augmentation, our NOC-based predictions from Φ_n enable more generalized feature learning, resulting in better pose alignment.

Method	#hypotheses	Retrieval Similarity↓
Φ_z + PC	8	0.111
Φ_z w/o Aug	8	0.082
Ours	8	0.075

Table 4. CAD retrieval ablation. Learning retrieval in the object canonical space (vs. camera space, denoted as PC) and with synthetic augmentation enables improved retrieval performance.

canonical space significantly improves retrieval.

How does object replacement augmentation affect retrieval and alignment? We illustrate the necessity of augmenting the synthetic scene layout with extra shapes (i.e., from ShapeNet [12]) in Tabs. 3 and 4. Both Φ_n and Φ_z trained on the augmented synthetic dataset improve significantly compared with ' Φ_n + w/o Aug' and ' Φ_z + w/o Aug' respectively, due to the increased diversity during training.

4.4. Limitations

While leveraging 3D perception through CAD model retrieval and alignment offers a compact representation of the scene, its efficacy for applications requiring exact reconstructions can be hindered by the absence of precise geometric matches in real-world environments. A potential approach to overcome this limitation involves deforming the extracted CAD models to enhance alignment with observations [20, 37]. Additionally, our approach does not model object relations explicitly, which could limit performance, since indoor scenes are often arranged in coherent global structures. Integrating considerations of scene context alongside object deformation represents a promising direction for achieving more accurate 3D perception.

5. Conclusion

We introduce DiffCAD, the first weakly-supervised probabilistic approach for single-image CAD model retrieval and alignment. By disentangling ambiguities in the monocular perceptual system through individual distribution modeling using diffusion, we effectively address uncertainties in scene depth scale, object shape, and pose. Notably, our diffusion models are trained only on synthetic datasets, and yet outperform the supervised state-of-the-art approach on real-world Scan2CAD image data [1], achieving a 5.9% improvement with only 8 hypotheses. We envision that this advancement will spur further progress in 3D probabilistic models, as well as 3D perception without necessitating real-world labels.

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6. Supplementary Material

6.1. Additional Results

We present additional qualitative results of our weakly-supervised approach on real-world ScanNet [1, 17]. Furthermore, we compare our method against ROCA [31] on the ARKit [6] dataset.

6.1.1 Qualitative Evaluation on ScanNet

In Fig. 7, we showcase our probabilistic reasoning for scene scale, object shape, and pose on ScanNet [1, 17]. We aggregate the hypotheses in the dotted boxes for each scene, illustrating that our approach yields multiple reasonable retrievals for CAD-based reconstruction, addressing ambiguities in object sizes.

6.1.2 Qualitative Evaluation on ARKit

Fig. 8 presents additional qualitative results on the ARKit dataset [6]. Our method demonstrates better robustness and accuracy in object retrieval and alignments across diverse images and object types.

Method	#hypotheses	bed	bkshlf	cabine	et chair	sofa	table	avg↑
$\Phi_n + P$	8	20.5	9.4	12.3	22.9	22.1	10.5	16.3
$\Phi_n + S$	8	20.5	14.3	12.9	29.3	27.8	14.6	19.9
Φ_n w/o Aug	8	23.0	12.8	24.5	45.3	37.3	12.0	25.8
Ours	8	28.6	16.7	32.8	55.0	41.1	18.6	32.1

Table 5. **Pose estimation ablation**. With synthetic data replacement augmentation, our NOC-based representation from Φ_n achieves more generalized feature learning, resulting in better pose alignment for all target categories.

Method	#hypotheses	bed	bkshlf	cabine	t chair	sofa	table	avg↓
$\Phi_z + PC$	8	0.105	0.088	0.155	0.115	0.093	0.108	0.111
Φ_z w/o Aug	8	0.080	0.077	0.081	0.085	0.069	0.097	0.082
Ours	8	0.075	0.064	0.079	0.075	0.066	0.089	0.075

Table 6. **CAD retrieval ablation**. Learning retrieval in the object canonical space (vs. camera space, denoted as 'PC') and with synthetic augmentation enables improved retrieval performance for our classes of interest.

Method	#hypotheses	bed	bkshlf	cabine	t chair	sofa	table	avg↓
Φ_s w/o \mathcal{E}_s	8	0.172	0.202	0.369	0.284	0.297	0.341	0.278
Ours	8	0.133	0.195	0.331	0.251	0.274	0.312	0.249

Table 7. Scene scale ablation. Encoding the feature from the depth map using \mathcal{E}_s enables better scene scale modeling for the target categories.

6.1.3 Further Ablations

CAD alignment ablation. We present category-specific evaluation results in Tab. 5, corresponding to Tab.3 in the main paper. Tab. 5 demonstrates that with synthetic data

augmentation and object NOC representation, our CAD alignment diffusion model Φ_n achieves superior alignment performance across domains for all categories.

CAD retrieval ablation. In Tab. 6, corresponding to Tab.4 in the main paper, we highlight the advantages of learning the retrieval condition in the canonical space, along with the benefits of synthetic data augmentation for the CAD retrieval diffusion model Φ_z .

Scene scale ablation. Tab. 7 compares our scene scale diffusion module Φ_s to a baseline approach without the feature extractor \mathcal{E}_s . We evaluate the scale prediction accuracy defined as $\mathbf{e}_s = \min_{\mathbf{i} \in \{\mathbf{N}\}} ||\mathbf{s}_{gt} - \mathbf{s}_i||_1$. Our design achieves a lower scale error compared to the baseline, indicating improved scale prediction accuracy.

6.2. Further Implementation Details

6.2.1 Data Preparation

Object mesh pre-processing. To encode CAD models into a compact latent space using Φ_o , we first canonicalize the original meshes from 3D-FUTURE [26] and ShapeNet [12] to have a normalized scale and consistent orientation. We save the scaling factor between the original and the canonicalized object for the synthetic data augmentation. Subsequently, we transform them into watertight meshes following the mesh-fusion process proposed in [74].

Synthetic dataset augmentation. We leverage the shape databases of objects from both 3D-FUTURE and ShapeNet, with a total of 18,229 objects. We substitute the original furniture of our target class within the 3D-FRONT layout. To achieve this, we randomly select an unused CAD model from the corresponding category in the database. Then, we scale the chosen object using the scaling factor of the original object, ensuring the preservation of object size balance in the augmented scenes. This augmentation process facilitates the learning from a more diverse set of object shapes and arrangements.

Synthetic data rendering. We employ BlenderProc [19] for our synthetic data rendering, generating RGB images, depth maps, and masks. Camera views are sampled by considering ray intersections with a minimum coverage of 15% of the object of interest, highlighting our focus on object-centric learning. Additionally, an off-the-shelf depth estimator, such as Zoedepth [9], is used to obtain depth estimates over the rendered color images. This information is necessary for calculating the target scale s by comparing predicted \mathbf{D} and rendered depth values \mathbf{D}_{gt} regarding Eq.5.

6.2.2 Network Architecture

Depth feature extractor \mathcal{E}_s . Fig. 9 diagrams the depth feature extractor network. We adopt the FCN-ResNet50 [54] and adjust its first convolution layer to take a single channel

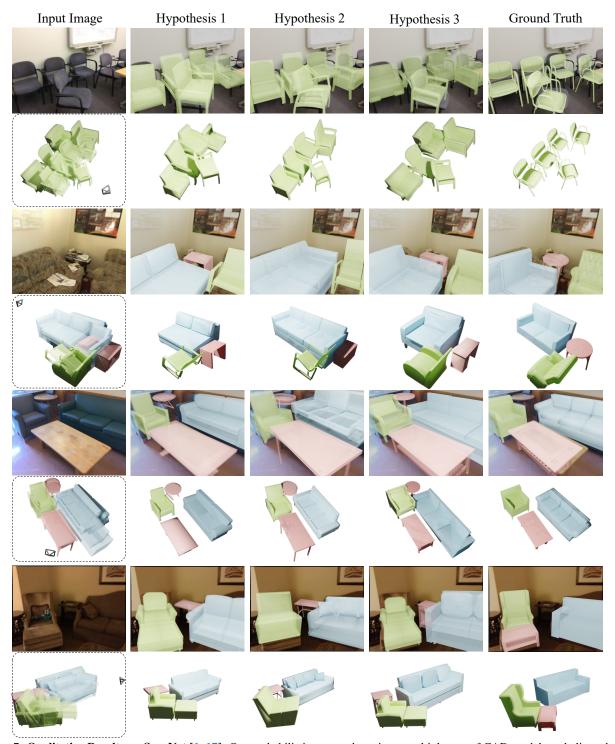


Figure 7. **Qualitative Results on ScanNet** [1, 17]. Our probabilistic approach retrieves multiple sets of CAD models and aligns them to our predicted scene scales. Our method achieves high-quality retrieval and alignment to cluttered scenes. Dotted: all three hypotheses, illustrating different scene scale reconstructions and addressing potential depth-scale ambiguities.

depth map as input, and use the feature before the final classification layer as the condition for the scene scale diffusion model Φ_s .

Object point cloud feature extractor \mathcal{E}_n **.** We utilize the GCN3D [52] as feature extraction backbone given the object point cloud **P** back-projected from masked depth map

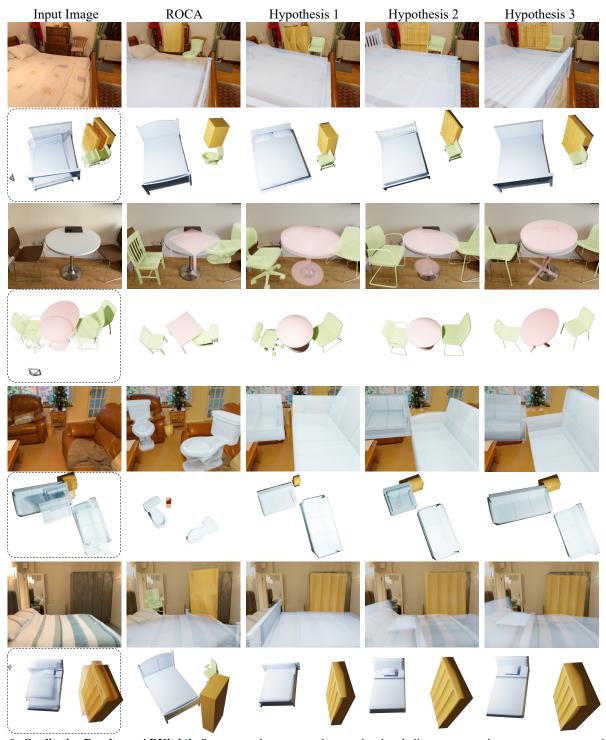


Figure 8. **Qualitative Results on ARKit [6].** Our approach presents robust retrieval and alignment to various scenes, reconstructing the scene with multi-feasible sets of object shape and pose pairs given the ambiguities in monocular perception. Dotted: The three hypotheses corresponding to the different scene scales.

 \mathbf{D}_p . Fig. 10 shows the object per-point feature extraction process, the feature then serves as input to the CAD alignment diffusion model Φ_n .

NOC point embedding \mathcal{P}_z . Given that NOCs inherently capture the observed object in its canonical space, we focus on learning the features of NOCs capable of distinguish-

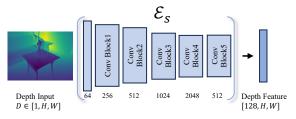


Figure 9. Overview of the Depth Feature Extractor \mathcal{E}_s . The feature extractor takes as input the predicted depth map, and processes it with hierarchical convolution blocks following [54], and outputs the extracted feature with the same spatial dimension as input. We indicate the feature dimension under each block.

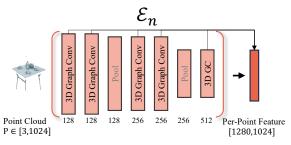


Figure 10. Overview of the Object Point Cloud Feature Extractor \mathcal{E}_n . The feature extractor takes the back-projected object point cloud as input, and extracts the per-point feature using GCN3D [52]. We indicate the per-point feature dimension below each 3D graph convolution block.

ing intra-class shape variations. To achieve this objective, we directly learn the feature embedding of NOCs through trigonometric mappings. Subsequently, a single-layer MLP is employed to project the per-point features into a 512-dimensional space. This NOC feature then serves as a condition for the CAD retrieval diffusion model Φ_z .

6.2.3 Test Split Generation

We introduce a new evaluation protocol for single-view CAD model retrieval and alignment on the ScanNet [1, 17]. Our per-frame test split is designed based on the validation set of the ScanNet25k image dataset, aligning with previous methods [31, 44]. For each target category, we first filter out the frames in which the centroid of the target object falls beyond the image plane. To avoid penalizing the heavily occluded objects, frames where the visible mask of the target object occupies less than 10% of the total image plane are also excluded. The visible masks are obtained by comparing the rendered depth map using ground truth pose with the original sensory depth map. In total, our test split contains around 2.5k images across the 6 target categories.

6.2.4 Used Open-Source Libraries

Our data pre-processing, model training and inference paradigm leverage several open-source libraries. Blender-proc [19] is employed for rendering synthetic data. The implementation of our model uses PyTorch. For the multihypothesis ranking scheme during inference, which includes rendering the retrieved CAD models using predicted poses, we utilize a PyTorch3D renderer [66].